

**ANURAG GROUP OF INSTITUTIONS**  
**(AUTONOMUS)**  
**I-B.TECH-II-SEMESTER-2017-18**  
**I-ASSIGNMENT TEST QUESTIONS**  
**SUBJECT: MATHEMATICS-II**

1. Evaluate (a)  $\int_0^1 x^5(1-x)^3 dx$       (b)  $\int_0^1 \frac{dx}{(1-x^3)^{\frac{1}{3}}}$       (c)  $\int_0^{\infty} 3^{-4x^2} dx$
2. Evaluate  $\int_0^{\infty} \frac{x^4(1+x^5)}{(1+x)^{15}} dx$  using B-Γ functions
3. Prove that  $\int_0^1 \frac{x^2}{\sqrt{1-x^4}} dx \times \int_0^1 \frac{1}{\sqrt{1-x^4}} dx = \frac{\pi}{4\sqrt{2}}$
4. Evaluate  $\int_0^{\frac{\pi}{2}} \sin^6 x \cos^7 x dx$
5. Show that  $B(m, n) = \frac{\Gamma(m)\Gamma(n)}{\Gamma(m+n)}$  where  $m > 0, n > 0$
6. Find  $L\left\{ \frac{\cos 2t - \cos 3t}{t} \right\}$
7. Find  $L\left\{ e^{-3t} \int_0^t \frac{\sin t}{t} dt \right\}$
8. Evaluate the improper integral  $\int_0^{\infty} e^{-4t} \sin 3tdt$  using Laplace transform
9. Find the Laplace transform of  $L\left\{ \int_0^t te^{-4t} \sin 3tdt \right\}$